

Research Status and Challenges of Restoring Force Models for Reinforced Concrete Components

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Abstract: The resilience model is an important tool for studying the seismic performance of reinforced concrete components. It describes the force-displacement relationship of components under external forces, reflecting the hysteretic behavior and energy dissipation characteristics, and providing a theoretical basis for seismic performance assessment. Based on existing literature, this paper systematically reviews the current research status of resilience models, analyzes key influencing factors such as material nonlinearity, geometric parameters, and loading paths, and discusses the main challenges in model research, including insufficient universality, complexity in characterizing nonlinear behavior, and lack of high-precision experimental data. To address these challenges, this paper proposes future research directions, emphasizing the improvement of model universality, the combination of experiments and numerical simulations to enhance model validation, and the further optimization of model efficiency and accuracy through multidisciplinary integration. The research results show that existing models have good applicability in describing simple conditions, but their performance in complex conditions is still limited. In the future, the practical value of resilience models in engineering seismic design needs to be enhanced through the coordinated development of theory and technology.

1. Introduction

The resilience model is a core tool for studying the seismic performance of reinforced concrete components. It describes the hysteretic behavior of components under external forces through the force-displacement relationship, and has become an important foundation for seismic response analysis and seismic design. With the increasing complexity and diverse demands of modern engineering, the existing resilience models have shown limitations in handling multi-directional loading, large deformations, and various nonlinear effects. Current research mainly focuses on the development and optimization of models under simple conditions, but the universality of the models, the precise characterization of nonlinear behaviors, and the lack of high-precision experimental data under complex loading conditions have restricted their further promotion and application. Therefore, it is of great significance to study the current status, challenges, and development directions of

resilience models. This paper aims to systematically review the research progress of existing resilience models, analyze the main bottlenecks in their practical engineering applications, and propose solutions from theoretical and technical perspectives to address complex conditions. By deepening the theoretical research and technical application of resilience models, their applicability in seismic design can be further enhanced, providing a solid scientific support for the seismic performance assessment of complex engineering structures.

2. Overview of Research on Restoring Force Models

2.1 Definition and Classification of Restoring Force Models

The restoring force model is a core tool used to describe the force-displacement relationship of reinforced concrete components under external forces. Its main function is to reveal the hysteretic behavior and energy dissipation characteristics of the components, which is an important part of seismic performance assessment. From a classification perspective, restoring force models can be divided into three types: empirical models, analytical models, and numerical models. These models are categorized based on their development methods and applicable scenarios. Empirical models rely on a large amount of experimental data and are usually developed for specific working conditions, with a narrower applicability; analytical models describe complex behaviors through mechanical derivation and can better represent the nonlinear performance of components; numerical models combine finite element methods to accurately simulate the restoring force characteristics of complex structures, especially suitable for large-scale seismic analysis. These models each have their strengths and weaknesses, and in engineering applications, they are usually selected based on actual needs.

2.2 Theoretical Foundations

The theoretical basis of restoring force models includes the nonlinear material characteristics of concrete and reinforcement, geometric parameters, and loading paths, among other factors. The cracking, crushing, and strain softening behavior of concrete are the main reasons affecting the shape of the component's hysteresis curve, while the yield and hardening characteristics of reinforcement directly determine the stiffness degradation and energy dissipation capacity in the mechanical response. Mander et al. (1988) proposed a nonlinear stress-strain model for concrete under compression, providing a theoretical basis for describing the cracking and softening mechanisms of concrete ^[1]; Menegotto and Pinto (1973) proposed a reinforcement cyclic loading model that more systematically reflects the reinforcement's hardening and degradation characteristics under cyclic loading conditions ^[2]. The slenderness ratio, cross-sectional shape, and reinforcement ratio of the component also significantly affect its mechanical properties. Loading paths and cumulative damage effects are key factors in hysteretic behavior; for example, complex loading under seismic action can lead to more pronounced energy dissipation and damage accumulation. Restoring force models must be based on these theoretical foundations, combined with experimental data and mechanical derivation, to accurately reflect the nonlinear behavior of components.

2.3 Research Progress

Research on restoring force models has gradually developed since the mid-20th century. Clough and Johnston (1966) developed the degrading bilinear model, introducing the characteristic of unloading stiffness degradation, which greatly improved its applicability ^[3]. In the 1970s, Takeda et

al. (1970) proposed the three-linear-segment model, which comprehensively described the hysteretic performance dominated by bending deformation^[4]. This model still has shortcomings in dealing with shear deformation and slip effects. Entering the 1990s, Dowell et al. (1998) proposed the Pivot model, which significantly enhanced the model's flexibility by setting key points to control stiffness degradation and pinching effects^[5]. Ibarra et al. (2005) proposed a hysteretic degradation model that can fully characterize energy dissipation from loading to collapse throughout the entire process^[6]. Numerical models based on finite element analysis have also become a research hotspot, with their accuracy and applicability continuously improving, providing important support for the seismic analysis of complex structures. The proposal and development of these models have provided important theoretical foundations and tools for simulating the nonlinear behavior of reinforced concrete components under seismic action. With the continuous increase in engineering demands, existing models still have certain limitations in dealing with complex conditions and require further research and improvement.

3. Key Factors Influencing Restoring Force Models

3.1 Material Properties

The establishment of restoring force models is highly dependent on the nonlinear performance of reinforced concrete materials. The nonlinear behavior of concrete, such as cracking, crushing, and strain softening effects, is key to the mechanical properties of the components. Cracking leads to a significant decrease in stiffness, while crushing affects the load-bearing capacity and energy dissipation performance of concrete. The emergence of softening effects causes the hysteresis curve to show a clear degradation characteristic during the unloading phase. At the same time, the yield and hardening behavior of reinforcement also play a decisive role in the hysteretic performance. The yield strength of reinforcement not only affects the initial stiffness of the hysteresis curve but also relates to the energy dissipation capacity of the component. Reinforcement exhibits unloading stiffness degradation and hardening characteristics during cyclic loading, and these phenomena together determine the restoring force characteristics of the component. The coupled effect of concrete and reinforcement performance makes the nonlinear representation of restoring force models particularly important under complex seismic conditions.

3.2 Geometric Parameters

Geometric parameters have a significant impact on the restoring force performance of reinforced concrete components. The aspect ratio, which is the ratio of the span to the height, directly affects the stiffness and deformation capacity of the components. A lower aspect ratio is usually associated with more significant shear deformation, while a higher aspect ratio is dominated by bending deformation. The reinforcement ratio also significantly affects the hysteretic performance; a higher reinforcement ratio can increase the load-bearing capacity and energy dissipation capacity of the components, but it may also lead to a decrease in ductility. The cross-sectional shape determines the distribution of stiffness and the failure mode of the components; for example, the differences in the distribution of bending moments and shear forces between rectangular and circular cross-sections can have different effects on the hysteresis curve. The combined effect of geometric parameters requires that restoring force models accurately reflect the influence of these key geometric characteristics when characterizing nonlinear behavior.

3.3 Loading Path and Cyclic Effects

Loading path and cyclic effects are significant factors affecting hysteretic characteristics. In actual seismic conditions, reinforced concrete components typically undergo complex loading paths, including positive and negative cyclic loading and asymmetric loading, which can lead to asymmetry in mechanical response and accelerated cumulative damage. The cumulative damage model proposed by Park and Ang (1985) deeply studied the impact of cumulative damage on the mechanical performance of components, pointing out that complex loading paths can significantly accelerate the damage evolution process ^[7]. Krawinkler's (1978) model of hysteretic behavior systematically analyzed the degradation laws of stiffness and strength of components under cyclic loading, revealing the coupled effect of loading paths and energy dissipation ^[8]. Changes in loading rate further affect the stiffness and energy dissipation capacity of components; inertia effects at high loading rates may lead to significant strength degradation. Cyclic loading effects alter the degradation patterns of stiffness and strength of components through cumulative damage, and the shape of the hysteresis curve will also change with the increase in the number of cycles. These factors require that restoring force models not only characterize the mechanical behavior under a single loading path but also fully consider the coupled effects of complex loading paths and cumulative damage under seismic action to enhance the applicability and accuracy of the model.

4. Key Challenges in Restoring Force Model Research

4.1 Insufficient Generality of Models

The lack of universality in restoring force models is one of the main challenges in current research. Most models are developed based on specific experimental conditions or scenarios, such as single deformation modes or specific types of components. This leads to difficulties in applying the models to complex structures or variable conditions, such as components with simultaneous bending, shear, and slip effects, or complex hysteretic behavior caused by asymmetric loading paths. Existing models show significant limitations when dealing with multidirectional loading (such as two-way or three-way vibrations in earthquakes) and large deformation effects. These limitations mainly stem from the targeted theoretical framework of the models, which lacks the ability to fully characterize complex nonlinear behavior. Therefore, improving the universality of models requires breakthroughs in fundamental theory, developing a unified framework that can comprehensively represent different deformation modes and loading conditions. The determination of model parameters should be more flexible to adapt to a wide range of engineering application scenarios, which is crucial for seismic design in practical engineering.

4.2 Accurate Representation of Nonlinear Behavior

Accurately characterizing nonlinear behavior is the core challenge affecting the precision of restoring force models. Concrete and reinforcement exhibit unloading stiffness degradation, strength degradation, and cumulative damage effects under cyclic loading, and the coupled action of these nonlinear characteristics significantly increases the complexity of the models. Unloading stiffness degradation affects the shape of the hysteresis curve, while the combination of strength degradation and cumulative damage can lead to significant load-bearing capacity reduction. Existing models are often only able to consider one characteristic in isolation and struggle to accurately describe their coupled effects simultaneously. This deficiency limits the model's comprehensive representation of complex nonlinear behavior. Therefore, establishing a restoring force model that can describe nonlinear behavior comprehensively requires the development of a coupled theory based on experiments and numerical analysis, along with multi-scale modeling

techniques to enhance the model's applicability and accuracy under various nonlinear effects.

4.3 Lack of High-Precision Experimental Data

The scarcity of high-precision experimental data limits the development of restoring force models, especially under complex conditions such as high strain rates and large displacement cyclic loading. In actual seismic actions, reinforced concrete components often experience extreme conditions, while most current experimental data focus on low strain rates and small displacement ranges, which fail to fully reflect the hysteretic characteristics under complex loading paths. The acquisition of experimental data under complex conditions is costly, and the limitations of technical levels of testing equipment and data collection methods further exacerbate this issue. This lack of experimental data directly affects the verification and optimization of models, leading to doubts about the reliability of models under extreme conditions. Therefore, strengthening experimental research and obtaining high-precision, wide-range experimental data is an important direction for future research and is also the foundation for the further development of restoring force models.

4.4 Multidisciplinary Integration

The integration of multidisciplinary approaches is a key breakthrough direction for enhancing the capabilities of restoring force models. With the development of artificial intelligence, big data, and machine learning technologies, these tools can significantly enhance the analysis of complex nonlinear behaviors and coupled effects. For instance, machine learning can train models on a large scale of experimental data, automatically recognize nonlinear relationships, and optimize parameters. Big data technology can integrate experimental and monitoring data from different sources, providing strong support for model calibration and validation. Multi-scale modeling techniques enable collaborative analysis between material, component, and structural levels, achieving a full-scale performance characterization from micro to macro. The integration of multidisciplinary methods not only improves the precision and efficiency of models but also further expands their applicability, especially in dealing with complex conditions and optimizing seismic design, showing great potential. This direction provides new ideas and technical tools for the development of restoring force models.

5. Future Development Directions

5.1 Enhancing the Generality of Models

Future research needs to focus on enhancing the universality of restoring force models to adapt to complex conditions and various types of components. Under multi-directional loading and large deformation, existing models often show insufficient accuracy or limited applicability, failing to fully reflect the mechanical characteristics of components. Therefore, optimizing existing models requires starting from the theoretical foundation and developing a framework for restoring force models that can uniformly describe different deformation modes and nonlinear behaviors. Model parameters should have greater adaptability, and through flexible parameter adjustments, they should be able to accurately describe the coupling mechanisms of different deformation effects such as bending, shear, and slip. Enhancing the universality of models will directly promote their application in seismic analysis of complex structures, improving the reliability and effectiveness of models in practical engineering.

5.2 Integration of Experiments and Numerical Simulations

Combining experimental and numerical simulations is a key approach to improving the accuracy and reliability of restoring force models. Future research needs to develop high-precision

experimental techniques to obtain experimental data under complex conditions such as high strain rates and large displacement cyclic loading, providing a foundation for model validation and optimization. Numerical simulation techniques, especially finite element analysis methods, can simulate complex loading paths and nonlinear behaviors when comprehensive experimental testing is not feasible. The concrete plastic damage model proposed by Lubliner et al. (1989) provides an effective theoretical framework for simulating the nonlinear behavior of concrete and has been widely used in the study of hysteretic behavior ^[9]. The application of OpenSees software in the validation of restoring force models, such as the simulation of hysteretic performance of shear walls and columns, further demonstrates the advantages of numerical methods.

The combination of experimental and numerical simulations can also effectively reduce experimental costs. Numerical analysis can assist in extrapolating experimental results and calibrating parameters, achieving mutual supplementation of experimental and simulation data. This combined approach can provide strong support for the accurate characterization of restoring force models under complex conditions. By integrating finite element models with advanced numerical algorithms, it is also possible to explore the dynamic response under complex seismic conditions more deeply, thereby significantly enhancing the applicability and reliability of restoring force models.

5.3 Multidisciplinary Collaboration

Interdisciplinary collaboration is a breakthrough direction for future research on restoring force models. Artificial intelligence technology can use machine learning algorithms to mine nonlinear relationships from a vast amount of experimental and numerical simulation data and optimize model parameters. Multi-scale modeling techniques can comprehensively depict the nonlinear behavior of concrete and reinforcement at the micro, meso, and macro levels ^[10]. Big data analysis technology, by integrating laboratory experiments, field monitoring, and historical data, provides richer and more comprehensive training and validation datasets for enhancing model accuracy. The combination of these technologies will significantly improve the applicability and reliability of models under complex nonlinear effects ^[11]. Through interdisciplinary collaboration, restoring force models can not only achieve higher precision and efficiency but also provide new technical means for seismic design and safety assessment. This research direction helps to promote the transition of restoring force models from theoretical research to broader engineering applications, providing strong support for the seismic performance optimization of complex engineering structures.

5.4 Expanding Engineering Application Scenarios

The future development of restoring force models should be closely integrated with actual engineering needs to further optimize seismic design solutions. In complex engineering such as high-rise buildings, bridges, and large-span structures, models need to consider more practical influencing factors, such as irregular components, construction defects, and multiple load effects ^[12]. Developing engineering-oriented restoring force models can enhance the practical applicability of models by integrating measured data, construction conditions, and field monitoring results. Seismic design requires fast and easy-to-use calculation tools; in the future, more efficient and user-friendly software should be developed to integrate advanced restoring force models into the engineering design process, aiding in the optimization and assessment of seismic performance for complex projects ^[13]. Expanding the application scenarios in engineering will maximize the practical value of the models.

6. Conclusion

As a core tool in the study of the seismic performance of reinforced concrete components,

restoring force models have made significant progress in describing the hysteretic behavior of components dominated by bending deformation. Faced with complex conditions and various types of components, existing models still show certain limitations^[14]. Especially in the representation of nonlinear behaviors such as multi-directional loading, large deformation, strength degradation, and slip effects, the precision and applicability of existing models need further improvement. Due to the scarcity of high-precision experimental data under conditions such as high strain rates and complex loading paths, the verification and optimization of models are challenging. Future research needs to address the following aspects: first, the universality of models should be enhanced by establishing a framework for restoring force models that can uniformly describe different deformation modes and various nonlinear effects; second, data support should be improved through the combination of experiments and numerical simulations to obtain high-precision data under complex conditions; finally, multidisciplinary methods such as artificial intelligence, big data analysis, and multi-scale modeling should be combined to break through technical bottlenecks in model parameter optimization and the representation of complex coupling effects^[15]. Through these efforts, restoring force models will serve the actual engineering needs more efficiently and accurately, contribute to the enhancement of seismic performance of complex structures, and provide important support for structural safety and stability.

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